



Verification Strategies for Feature-Oriented Software Product Lines

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⇒ automotive, aircraft, ...

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- Verification of feature-oriented SPLs

Problem: Scalable Verification

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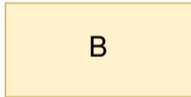
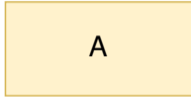
{A}

{B}

{A, B}

Product-Based

Problem: Scalable Verification



Feature-Based



{A}



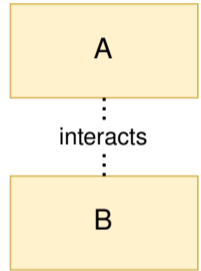
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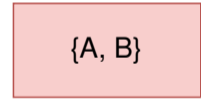
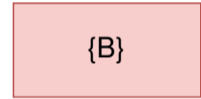
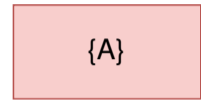
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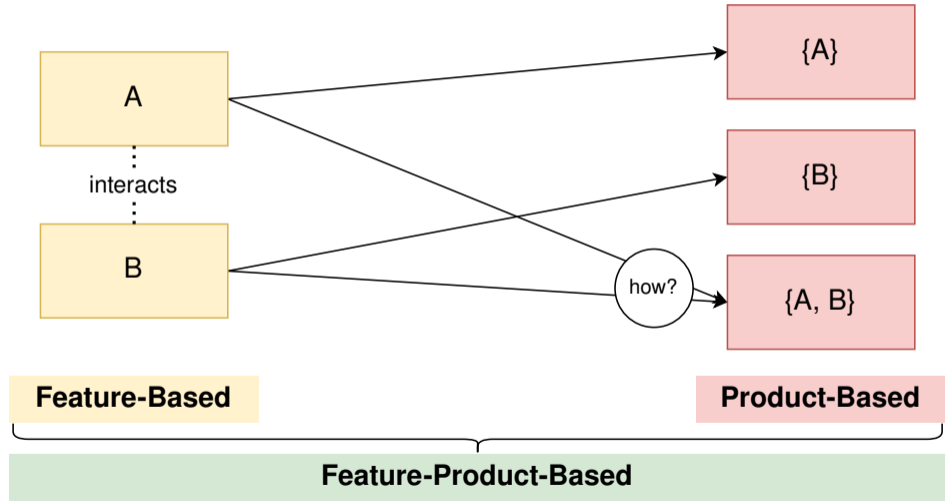


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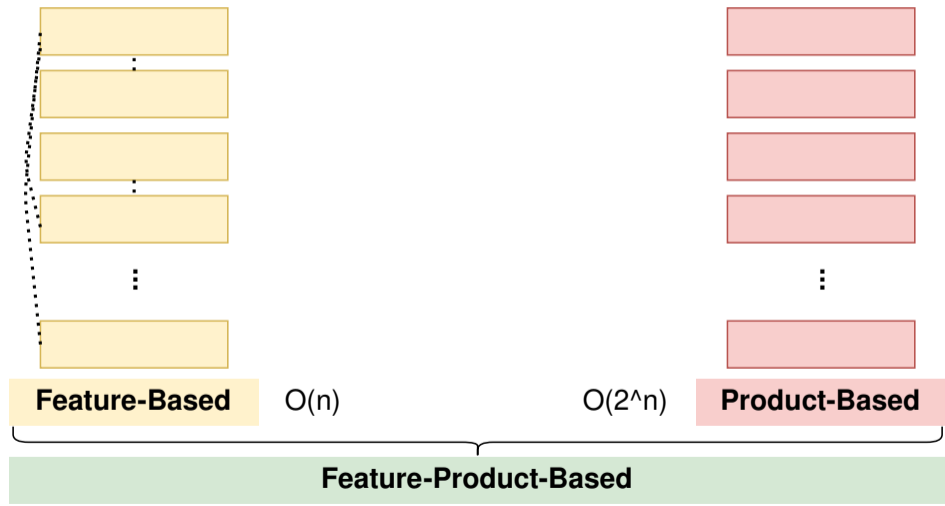


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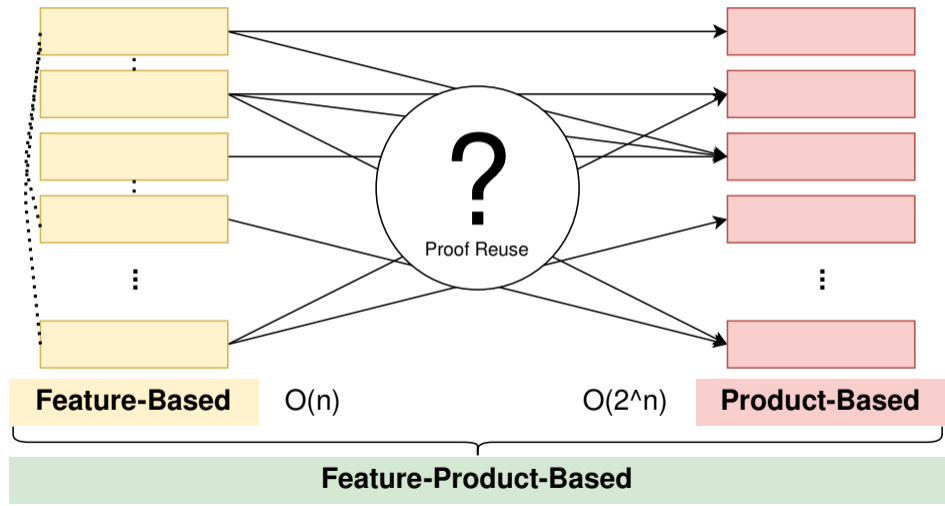
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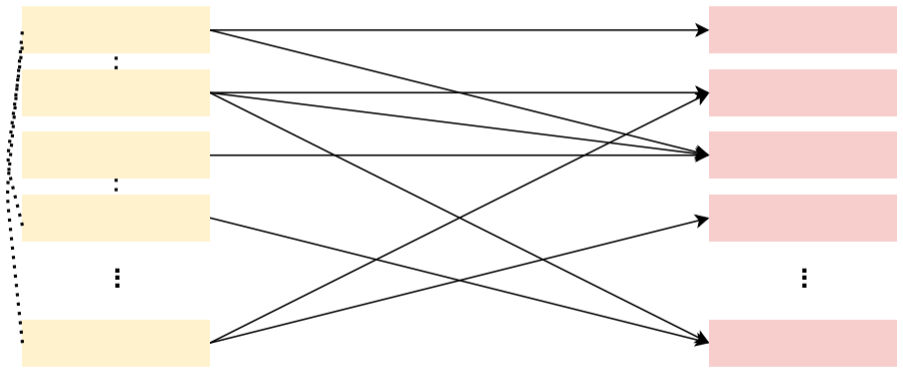




Two Opposing Solutions

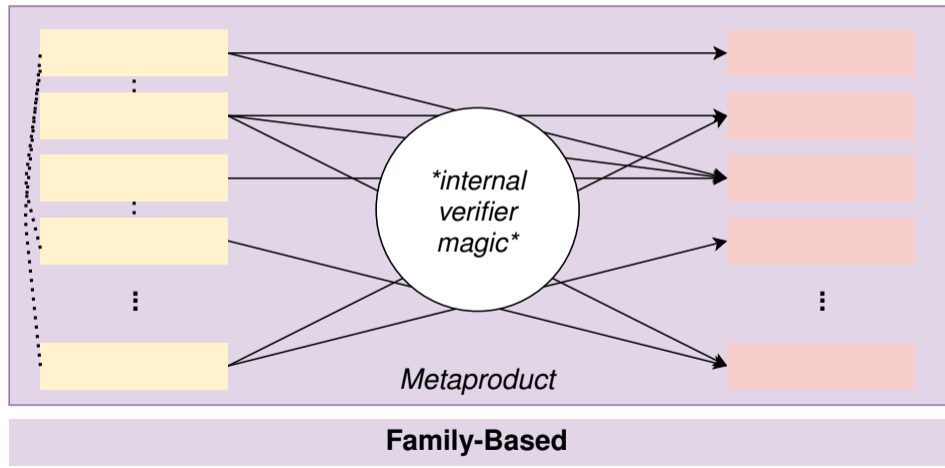
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Solution 1



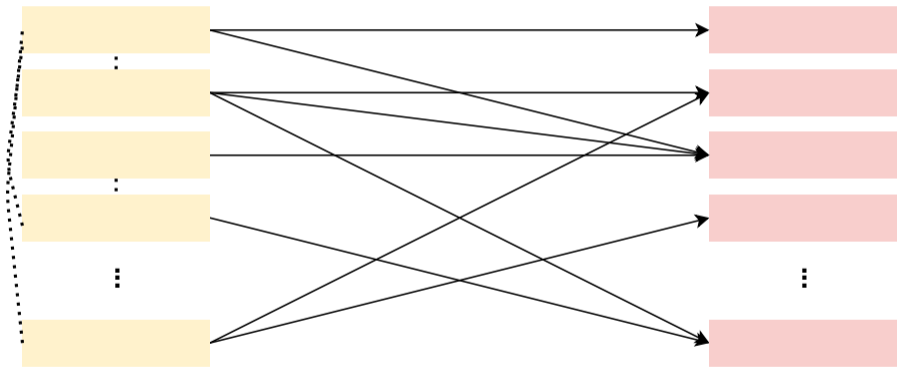
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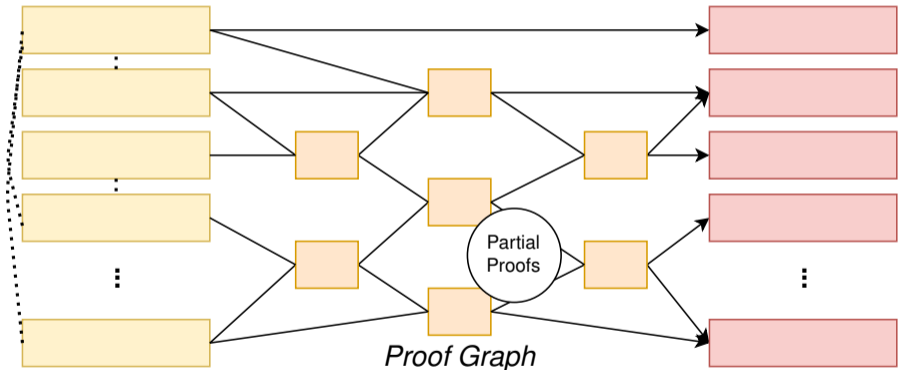
Two Opposing Solutions

Solution 2



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Feature-Family-Based



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⇒ A novel technique for verification of FOP-based SPLs

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- **Goals:**
 - ⇒ Align proof reuse with software reuse by small, modular proofs
 - ⇒ Position proof plans as manipulatable, first-class objects

Proof Reuse with Partial Proofs

$\text{ins}(A, x): \{A \text{ is sorted}\}$

$\text{original}(A, x); \text{sort}(A)$

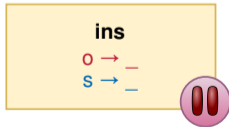
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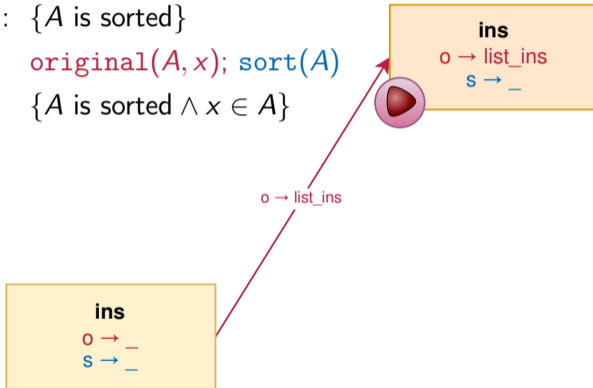


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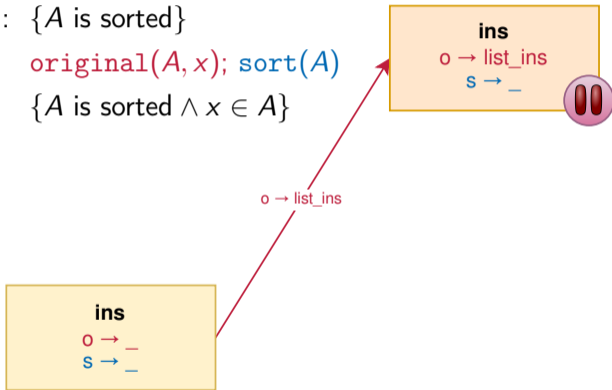
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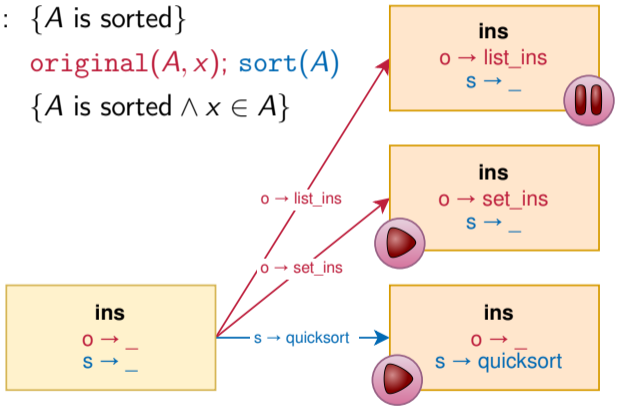


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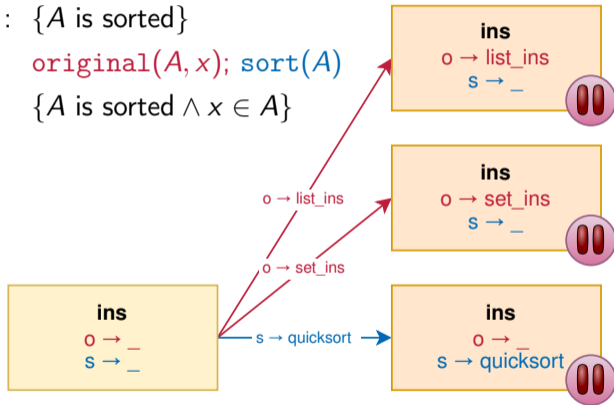


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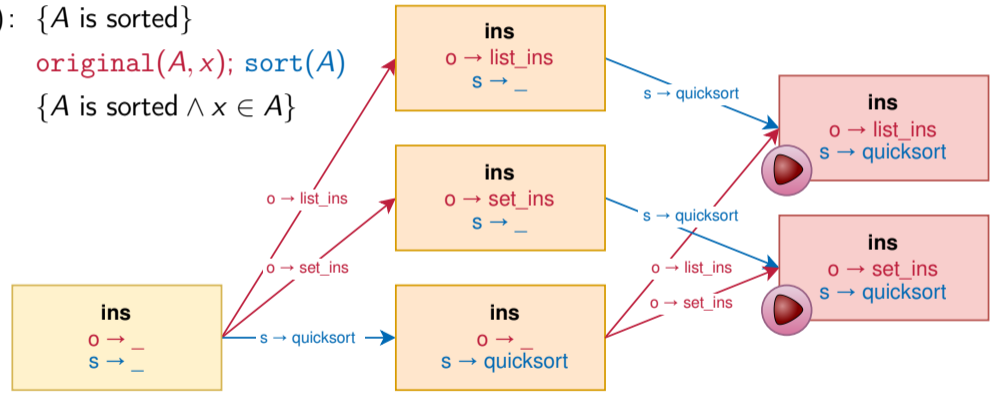
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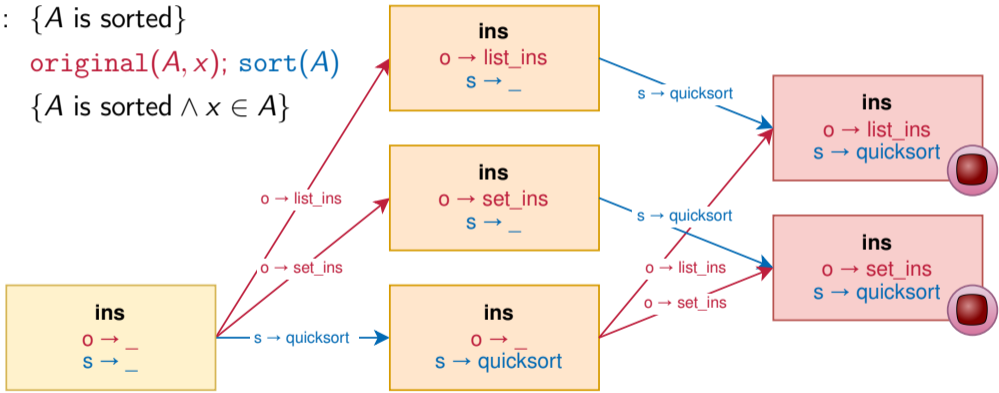
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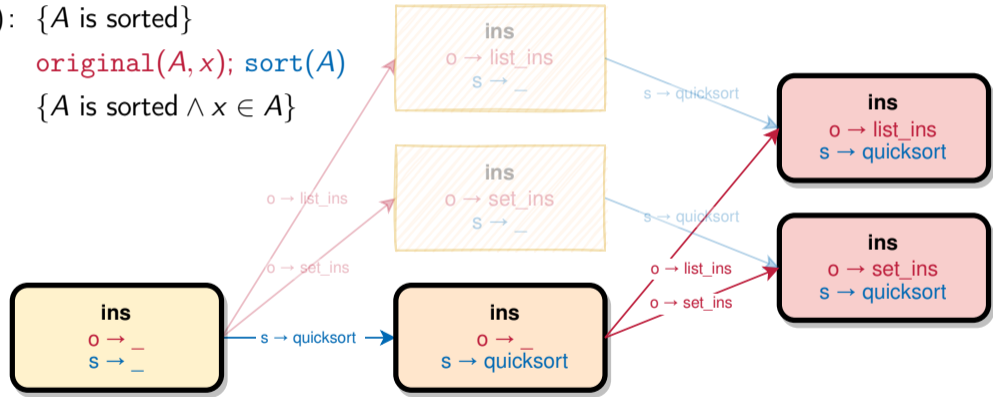
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Proof Plan with Reuse

An SPL and its Proof Graph

An SPL and its Proof Graph

| | List | Set | Ord |
|------|------|-----|-----|
| ins | ● | ○ | ○ |
| find | ● | × | ○ |
| sort | × | × | ○ |

{List}

List
ins

List
find

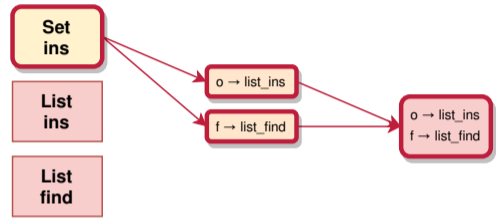
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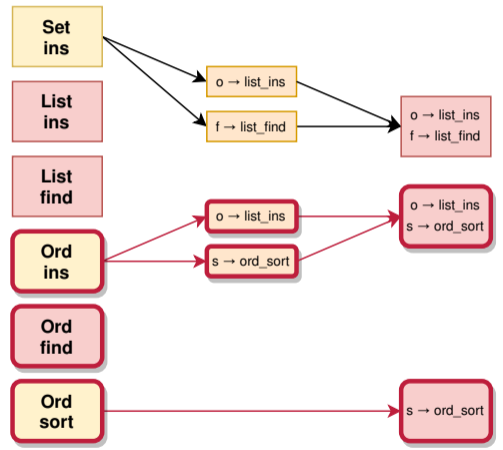
{List}

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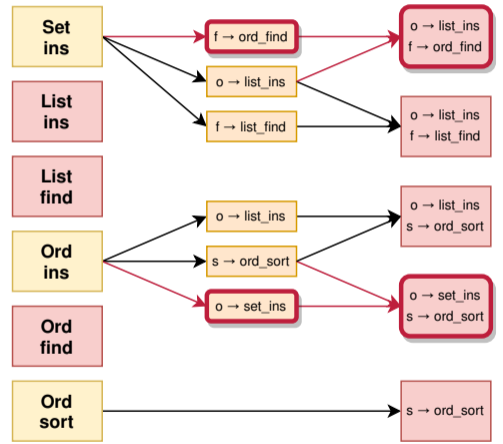
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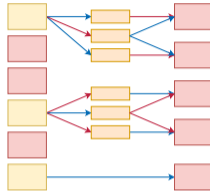
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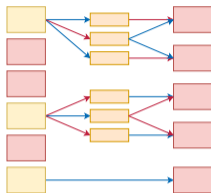
A Spectrum of Verification Strategies

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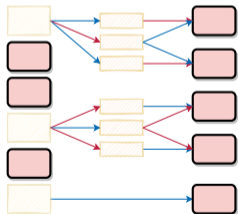


Proof Graph

A Spectrum of Verification Strategies

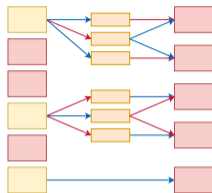


Proof Graph

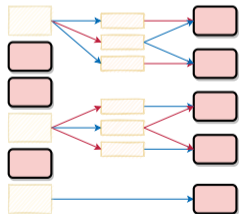


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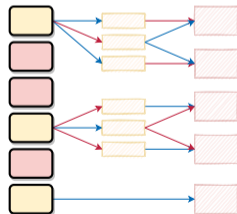
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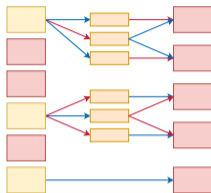


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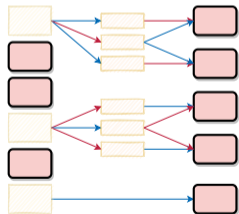


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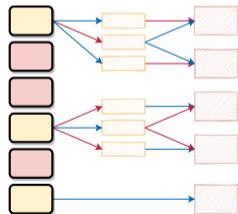
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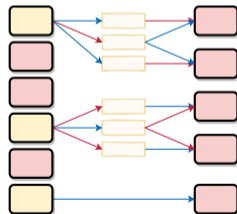
Proof Graph



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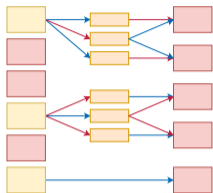


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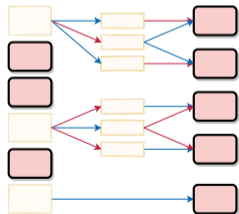


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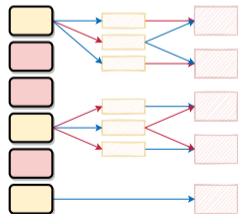
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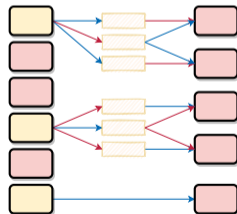
Proof Graph



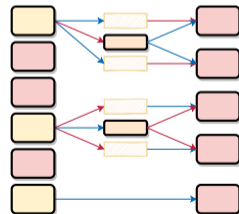
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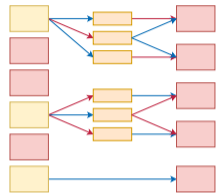


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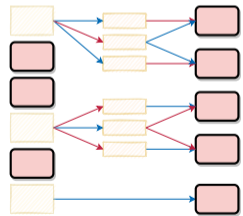


Feature-Family-Based*

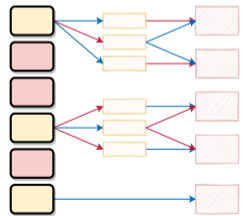
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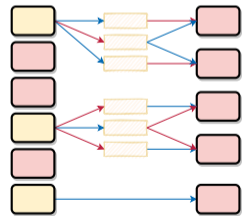
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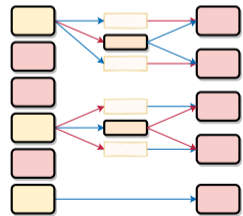
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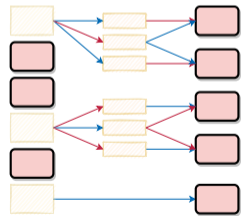
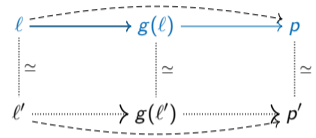


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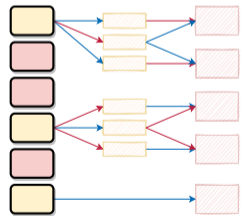
* How to choose well?

A Spectrum of Verification Strategies

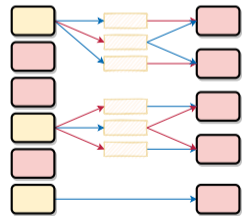
Applications



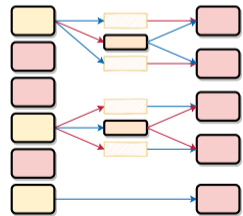
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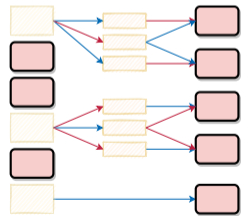
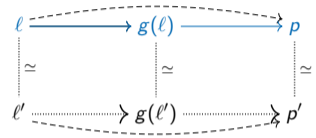
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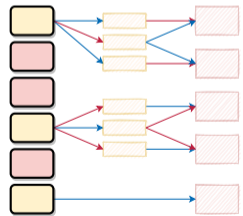
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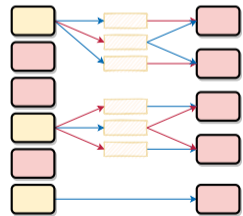
- Post-Hoc Verification



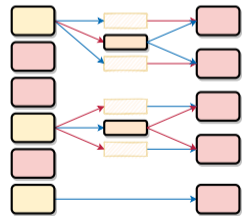
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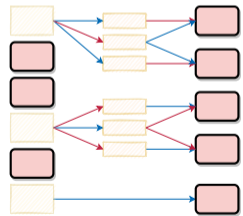
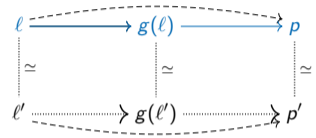
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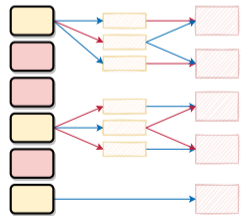
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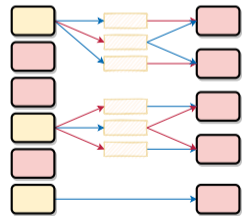
- [Post-Hoc Verification](#)
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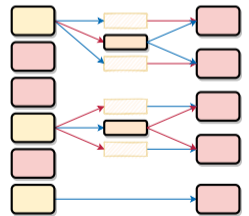
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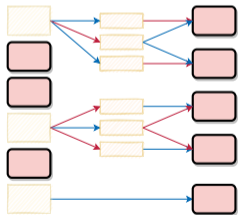
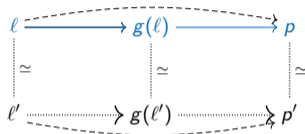
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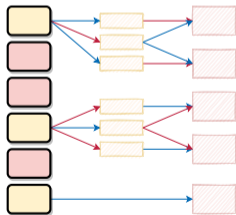
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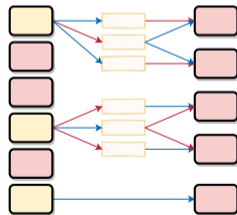
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- Evolution Scenarios
- Lazy Exploration*



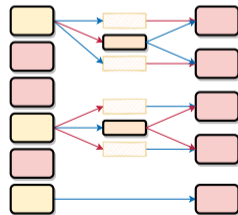
Product-Based



Feature-Based



Feature-Product-Based



Feature-Family-Based*

* How to choose well?



¹<https://github.com/ekuiter/KeYP1>

- **Subject:** *List* case study¹
⇒ Java + JML + FeatureHouse, 5 features, 13 methods

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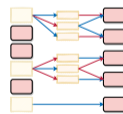
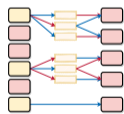
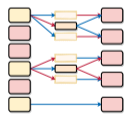
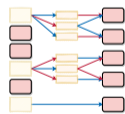
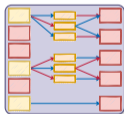
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| <i>Verification strategy</i> | <i>Time [s]</i> |
|------------------------------|-----------------|
| Family-Based | 20.0 |
| Product-Based (dup) | 23.7 |
| Feature-Family-Based | 26.2 |
| Feature-Product-Based | 28.8 |
| Product-Based (dup) | 157.7 |

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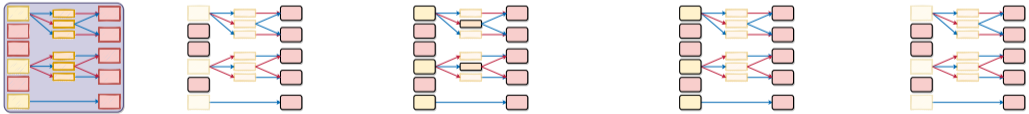


Family-Based > Product-Based > Feature-Family-Based > Feature-Product-Based ≫ Product-Based (dup)

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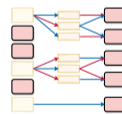
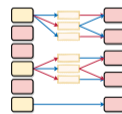
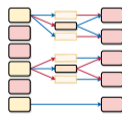
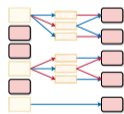
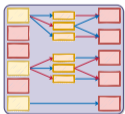
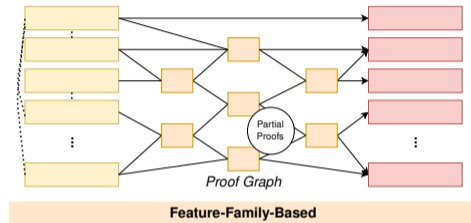
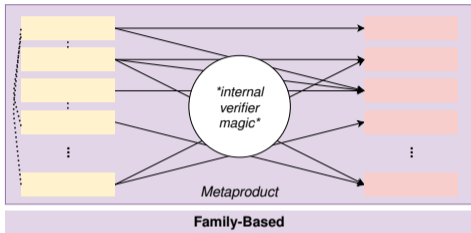
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Threats to Validity?

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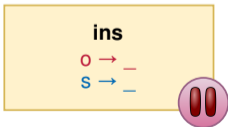


Family-Based > Product-Based > Feature-Family-Based > Feature-Product-Based ≫ Product-Based (dup)

$\text{ins}(A, x): \{A \text{ is sorted}\}$

$\text{original}(A, x); \text{sort}(A)$

$\{A \text{ is sorted} \wedge x \in A\}$



```

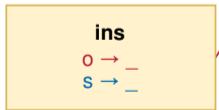
/*@ requires sorted(A);
   @ ensures sorted(A) && contains(A, x); */
void main(int[] A, int x) {
    original(A, x);
    sort(A);
}

/*@ model boolean original_requires(int[] A, int x);
   @ model boolean original_ensures(int[] A, int x); */
void original(int[] A, int x);

/*@ model boolean sort_requires(int[] A);
   @ model boolean sort_ensures(int[] A); */
void sort(int[] A);

```

$ins(A, x): \{A \text{ is sorted}\}$
 $original(A, x); sort(A)$
 $\{A \text{ is sorted} \wedge x \in A\}$



$o \rightarrow list_ins$



```

/*@ requires sorted(A);
   @ ensures sorted(A) && contains(A, x); */
void main(int[] A, int x) {
    original(A, x);
    sort(A);
}

/*@ model boolean original_requires(int[] A, int x) { return A.length > 0; }
   @ model boolean original_ensures(int[] A, int x) { return contains(A, x); } */
void original(int[] A, int x);

/*@ model boolean sort_requires(int[] A);
   @ model boolean sort_ensures(int[] A); */
void sort(int[] A);
    
```